### Intensive English Language / New Arrivals Program Mathematics and Numeracy: Teaching Learning Sequence

**Strand** Number and algebra

**Sub-strand** Fractions and decimals

**Levels** ABCD

Reception, Year 1, Year 2, Year 3

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#### Use this units with your own student cohort

Teachers are invited to trial and modify this teaching learning sequences. Content may need to be modified to meet the particular learning needs of a student cohort.

Designers started with the same template, and while there was broad agreement on the use of the template – there may be some variations between this Teaching Learning Sequence and other Teaching Learning Sequences that were developed by DECD educators.

- differentiated activities may be found in either the activities column or the evidence and differentiation column
- generally, language elements were not repeated once they were recorded in an earlier activity
- cross curriculum priorities are included in some unites but not in others.

A feedback form is available at tiny.cc/IELP-NAP-TLS. Please forward feedback to Erika Vonaspern



<sup>1 |</sup> Number and algebra: Fractions and decimals | Reception, Year 1, Year 2, Year 3 | Intensive English Language / New Arrivals Program | http://tiny.cc/IELP-NAP-TLS Mathematics and Numeracy Teaching Learning Sequence | Contributed by: Lousie Bradshaw and Koon Lee

# Intensive English Language / New Arrivals Program Mathematics and Numeracy Teaching Learning Sequence

WHAT DO WE WANT STUE	WHAT DO WE WANT STUDENTS TO LEARN?						
Strand: Number and Algebra Substrand: Fractions and Decimals		Learning Goals					
		Achievement Standards		Content Descriptions	Proficiencies		
Mathematics Levels:  ABCD  (Year R, 1, 2, 3)	Time Line:	A		<ul> <li>A Recognise a whole and parts of a whole in everyday contexts</li> <li>A Recognises that a whole can be divided into equal parts</li> <li>A Identifies quantities such as more, less and the same in everyday comparisons.</li> </ul>	The student demonstrates the following proficiencies.  Understanding  Connects fractions to real life experiences  Sees the connection		
Overarching Ideas There are numbers between whole numbers.  We can express these quantities using fractions or decimals. Wholes can be divided/ shared into equal parts and can be expressed as fractions.  Fractions can also be used to express ratios and relationships between quantities.		В	Identifies representations of one half.	<ul> <li>B Recognise and describe one half as one of two equal parts of a whole.</li> <li>B Explores the naming pattern for fractions (no. of pieces relates to the name. 6 pieces equals sixths)</li> </ul>	<ul> <li>between fractions and other symbols that represent how many.</li> <li>Defines a fraction</li> <li>Fluency</li> <li>Identifies quantities using</li> </ul>		
		C	Divides shapes into halves, quarters and eighths Divides collections into halves, quarters and eighths  Models and represents unit fractions	<ul> <li>C Recognise and interpret common uses of halves, quarters and eighths of shapes and collections.</li> <li>C Make the connections between the increasing number of parts to the decreasing size of parts.</li> <li>C Explores the different ways of representing fractions using symbols, words and diagrams (halves, quarters, eighths)</li> <li>C Visualises halves and quarters</li> <li>D Model and represent unit fraction, including ½, ¼, 1/3, 1/5 and their multiples to a complete whole.</li> </ul>	more, less and the same.  Reasoning Generalise the naming pattern of fractions.		

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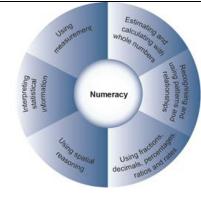
#### WHAT DO WE WANT STUDENTS TO LEARN?

#### Numeracy General Capability

Interpreting and Applying Proportional Reasoning

#### Level1a

Students recognise a whole and parts of a whole in everyday contexts



#### Level 1b

Students recognise that a whole object can be divided into equal parts and can identify quantities in every day comparisons (more, less, same)

#### Level 2

<u>Students visualise and describe halves and quarters and solve problems using them.</u>

#### Other General Capabilites

Literacy The literacy capability of *Composing Texts* is guided by and reported in the sequence of the IELP Progress Report. In addition, the following aspects of the *Comprehending Texts* continuum are taught and assessed.

#### Level 1e

- Navigate, read and view learning area texts with familiar vocabulary and supportive illustrations
- Listen and respond to learning area texts (brief questions, one and two step instructions, and listen for information in simple spoken texts)
- Interpret simple texts using comprehension strategies

#### Level 2

- Navigate, read and view learning area texts with illustrations and simple graphics
- Listen and respond to learning area texts (two or more step instructions)
- \_Interpret and use texts to gather information and make some obvious inferences

#### Critical and creative thinking

#### Level 2

- Pose guestions to explore issues, and compare information in their world
- Identify and describe familiar information and ideas during a discussion or investigation
- Build on what they know to create ideas and possibilities in ways that are new to them
- Describe thinking and learning strategies, with support.

Diagnostic Assessment: (What do the students bring?) How are you going to find out?	Assessment of Learning summative	Assessment as Learning Self & peer assessments	Assessment for Learning Formative
riow are you going to find out.	Brainstorm students' ideas	Explain ideas to peers and teacher	Brainstorm students' ideas
Assess understanding of the concept of whole by sorting/ identifying whole objects, collections, shapes and measures.  Investigate understanding of equal and unequal Assess understanding of what a fraction is	Drawings and photographs to demonstrate understanding  Written/ picture evidence  Use symbols and notation and apply	Inquiry and clarification of understanding of concepts  Pair share- discussing, evaluating own and partner's understanding	Anecdotal evidence of understanding  Written/ photographic evidence  Label equal and unequal quantities,
Be able to name fraction pieces(1/10, 1/5,1/8)	knowledge to activities  Be able to explain and represent a fraction  Complete fraction naming activity	Ability to complete task independently  Record and represent what a fraction is  Identify and label fraction pieces	pieces, areas  Oral retell and demonstration of what a fraction is  Identify fraction names and be able to match the diagrams
		Top 5  Lawrey Class  Top 1  Lawrey Class  Lawrey Class  Lawrey Committee  Lawrey Com	

#### KEY

Content Descriptions are in plain font Achievement Standards: Bold font

Numeracy Learning Continuum Description. Underlined font

WHAT DO WE WANT STUDENTS TO LEARN?	WHAT WILL WE DO	TO GET THERE?		HOW WILL WE KNOW IF THEY'VE LEARNT IT?
Mathematical Skills and Concepts	Sequenced learning activities	Language Elements	Resources	Evidence and Differentiation
A- Recognises a whole and parts of a whole in everyday contexts	1- UNDERSTANDS EQUAL PART / WHOLE Gathering Prior Knowledge  Activity 1.1 Ask the students, what is a fraction? Discuss when you might need to use fractions. Get them to think, pair share to access their existing knowledge. Display the definition – 'a fraction is an equal part of a whole'. Explain that you are going to explore equal part and whole.  Activity 1.2 Display the four different kinds of wholes (shapes/regions, objects, collections and measures) and explain that you are going to be an "Equal Part Detective" for each one of these wholes. Talk through with the class what they think equal means (same as). Put the four activities out on four different tables and students rotate through them in pairs. Set up the tables as follows.  Shapes – Give students an A3 piece of paper which has a range of regular and irregular shapes on it, some of which have been divided into unequal parts. Give each pair of students some sticky labels with the words FRACTION – EQUAL PARTS written on them. They have to stick the label on the ones they think meet the definition of a fraction	Participants: Whole, part of a whole, equal part, fraction, collection, shape, size, quantity  Describers: equal, unequal  Processes:: explore, notice explain, identify, label  Commands: Explore the activities on the table. Identify and label the fractions. Explain your choices.  Simple sentence: This is a fraction.  Complex sentences: These are fractions because they are divided into equal parts, quantities or measures.  Tense: simple present tense.	Watch 'Investigating halves of familiar objects-Splash ABC  splash.abc.net.au/home# !/media/29646/  2D shapes, 3D objects, counters, unifix cubes, pop sticks containers eg. cups classroom objects eg rulers, pencils  A3 paper with pictures of 2D shapes Sticky labels with equal parts written on them.	□ I can recognise a whole or equal parts.  Needs support then continue to explore this concept focusing on length models, such as Cuisenaire Rods.  Virtual Cuisenaire Rods can be found at <a href="http://nrich.maths.org/4782">http://nrich.maths.org/4782</a> Needs extension then extend the range of shapes, objects, collections and measures. <a href="http://www.scootle.edu.au/ec/search?accContentId=ACMNA058">http://www.scootle.edu.au/ec/search?accContentId=ACMNA058</a>

Key learning: A fraction of a shape has equal size.	Participants: classroom objects- ruler, eraser,		
Objects - On this table you have a basket of everyday 3D objects where you have used a texta/tape to mark parts on them, some of which have been divided into equal parts, some which have been divided into unequal parts. Give each pair of students some sticky labels with the words FRACTION – EQUAL PARTS written on them. They have to stick the label on the ones they think meet the definition of a fraction.	pencil container , ball	Assortment of objects with parts marked on them.	
Key learning: A fraction of an object has equal size.	Participants : unifix cubes, counters, popsticks,		
Collections – On this table you have an A3 piece of paper which has a number of collections on it, some of which have been divided into equal parts, some which have been divided into unequal parts. Give each pair of students some sticky labels with the words FRACTION – EQUAL PARTS written on them. They have to stick the label on the ones they think meet the definition of a fraction	buttons	Sticky labels Collections of counters, popsticks, bottle tops	
<b>Key learning</b> : A fraction of a collection has, equal quantity (how many).			
Measures – have a photo of the school oval, the basketball court, a cup, a jug which have had parts marked on them with a texta (some equal/unequal) Give each pair of students some sticky labels with the words FRACTION – EQUAL PARTS written on them. They have to stick the	Tense: simple present tense. I see the basketball court has 3 equal parts.	School oval, basketball courts, cups, jugs with tape or texta marks	
label on the ones they think meet the definition of a fraction.  Key learning: A fraction of a measure has equal size.	Visual Literacy equal and unequal symbols = and ≠		
Introduce the = and ≠			

A - Recognises that a whole can be divided into equal parts	2EQUAL AND NOT EQUAL- Divide fruit loops between students (focus on amount). Do they have the same? How can we make sure that everyone has the same amount, that it is equal? Ask groups of students to divide other collections such as counters and textas so that the students can gauge whether they have been divided equally. Show the students shapes that have been cut into parts, are the parts equal? How do we know? Brainstorm suggestions. Articulate which part is equal.	Processes: divide, share, count out, brainstorm  Describers: equal, unequal  Circumstance: divide equally	Fruit loops/ cheerios counters, textas	□ I can recognise that a whole can be divided into equal parts.  Needs support Then provide tasks where students explore equal share of area, shape, other collections and measures. Share a jug of liquid equally between 3 people.  Needs extension Students repeat activity with other materials. Vary the quantity or number of groups Eg collection of marbles given to 7 students.
A - Identifies quantities such as more, less and the same in everyday comparisons.	3. MORE, LESS OR EQUAL  Using the 4 tables of activities as in activity 1, explore more or less in each of these contexts. For example using sticky labels on the Collections table, label more or less or the same for the collection shown.	Comparative Language: more than, less than, same as		□ I can compare quantities of everyday resources.  Needs support Then reduce number of distractions that students may be attending to e.g. share less of any item.  Needs extension Then attempt Studyladder interactive activities for comparing groups.  www.studdyladder.com.au

B - Explores the naming pattern Use Interactive □ I can name fractions. 4 EXPLORES THE NAMING PATTERN FOR **Technical Vocabulary:** for fractions whiteboard to flash Naming pattern FRACTIONS. **Needs support** equal parts. sixths, sevenths etc. Then practise ordinal numbers. Explain that when the mathematicians were inventing Use a calendar for the naming Processes: fractions and how they worked, they came up with a pattern. action: name naming pattern that would make it really easy to remember relational: equals, is However many equal parts there are – that's what they are Needs extension mental: think called. Then explore the larger the verbal: is called number of equal parts, the Eq: 6 equal parts > sixths, 28 equal parts? Twenty eighths **Compound Sentences:** smaller the size of the part. Engage the students in the pattern. Eg: flash on the screen There are x equal parts so 10 parts would be called each part is called a \_\_\_\_. Only do it for those that follow the pattern. When students Embedded clause A are fluent with this, introduce the anomalies – ie. which whole (which is) divided ones are exceptions to the pattern- '1ths, (firsts)2ths into 12 parts has 12 (halves), 3ths, (thirds), fourths and quarters, twelfths. **Complex Sentences:** I think this is a fifth because there are 5 equal parts. Fractions have 'th' added to the number, but not fractions that end in 1,2,3. View video ABC □ I can explain the connection 5. RELATIONSHIP BETWEEN DENOMINATOR AND **Technical Vocabulary:** C - Makes the connections between number of parts and relates, denominator, between the increasing number **FRACTION SIZE** Splash.abc.net.au size of the parts. of parts to the decreasing size Comparatives: bigger, Activity 5.1 of parts. smaller, Visually show the students that the number of equal pieces **Needs support** in a whole relates to the fraction name. Use fraction pies. Sentence Structure Then expose the children to Compare the denominator to the size of the part. Paired constructions with more fraction pies. Use grid verb to be omitted. paper for folding into halves and Paper dividing. Give students strips of equal sized paper. The larger the Start by folding one into 2 equal parts, the next into 4, then quarters. denominator, (is), the into 8. Write the symbol. Notice that the bigger the smaller the fraction (is) denominator, the smaller the part. Stick strips into maths Needs extension Explore other constructions books to demonstrate concept. What do students notice?

eq The smaller the pizza,

Then fold paper into thirds,

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	Give students shapes such as circles, squares and collections such as egg boxes, write the symbols.	the less we all eat.  Processes: write, discuss,	sixths and twelfths.  Play Fraction Matcher –
	concentrations such as egg boxes, write the symbols.	use	(differentiated levels)
B - Recognise and describe one half as one of two equal parts of a whole.	Activity 5.2 Students work in pairs, divide collections of objects or shapes into equal parts, write the fraction name on each part, discuss what you notice about the number of parts and the size of the part./ collection . Use sharing mats for collections (eg: divide A3 paper into 3 equal parts for students to share thirds of a collection.	Technical Vocabulary: sharing mats	www.topmarks.co.uk (fractions)
C - Explore the different ways of representing fractions using symbols, words and diagrams (halves, quarters, eighths)	Activity 5.3  Students work in pairs. You give each pair the same Shape/ object/ collection/ measure but ask each pair to show you a different fraction on that Shape/ object/ collection/ measure eg: halves, thirds, fourths, eighths, tenths  Get them to share. Is there anything they can notice? What would be their theory? Can they prove their theory?		<ul><li>5.2 could be a formative assessment.</li><li>5.3 could be a summative assessment.</li></ul>
C. Divides shapes/objects into halves, quarters and eighths.	<ul> <li>6. ONE WHOLE: DIFFERENT WAYS OF PARTITIONING</li> <li>Activity 6.1</li> <li>Students select a shape, object, collection, measure (one of each) – show me at least three fractions for each WHOLE. EG: you might set up four tables one for each WHOLE. Students rotate through the tables, at each table they show three ways of making fractions for that WHOLE. They then have to describe</li> </ul>	Technical Vocabulary: half, halves, investigate, justify  Processes: select, describe, show, justify, investigate,  Compound sentences: Here is my whole shape	This could be a formative assessment.  Needs support Then investigate Scootle activities for showing halves
C. Divides collections into halves, quarters and eighths	what they have done. Eg: here is my WHOLE shape (a regular hexagon), I divided it into quarters  Activity 6.2  Provide students with at least one of each kind of WHOLE, and ask them to show you half with that whole. Students justify their thinking to a partner.	and I divided it into quarters etc.  Complex sentence: This is a half of a whole because	Needs extension Then extend the challenge by providing more complex wholes to partition and into different parts. Diagnostic testing on halves and quarters (Fixing Misconceptions in

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	Ear This is a half hosqueo		
	Eg: This is a half because		Fractions by Tierney Kennedy)  Tick all the pictures that represent quarters and halves.  Appendix 1
D. Represents a fraction of a whole	7. REPRESENTS FRACTIONS  Revisit the previous task of making fractions but this time the emphasis is on them naming the parts.  Model and explain the three conventions for representing fractions eg: symbol (numerator /denominator /vinculum) and number name (fourth)  Eg: Students pick a shape, an object, a collection, and a measure (one of each) – show me at least two fractions for each WHOLE and label its parts. Eg: you might set up four tables, one for each WHOLE. Students rotate through the tables, at each table they show two ways of making fractions for that WHOLE. They then have to describe what they have done. Eg: Here is my WHOLE shape (a regular hexagon), I divided it into quarters.	Technical Vocabulary: numerator, denominator, vinculum, Processes: model, explain, describe, show, write, demonstrate	
	8. EXPLORES THE RELATIONSHIP BETWEEN PARTS AND WHOLE AND NAMING  Provide students with a fraction kit that doesn't have the pieces named (or alternatively pieces of felt/paper that have been cut up to have proportional relationships) Ask them to choose a fraction piece – what is the value of each of the other pieces to make a whole? Label each piece.	Technical Vocabulary: select, theory, Processes: choose, label, explore, prove	

they know it is? Write the fraction notation on the board & then working in pairs show 1/2 in as many ways as they way ways as they way ways as they way ways as they way way ways as they way way ways as the way	B	8- Students visualise and describe halves and quarters and solve problems using them	then working in pairs show 1/2 in as many ways as they can think either by drawing or using materials. Check that the 2 parts in each representation are equal. Repeat for ¼.  Using small white boards, students draw then divide a shape into quarters, check the shapes are divided into quarters equally.  Create a fraction poster which represents ¼ of collections.	quarter/ fourth  Complex sentences: I know this is a half because		www.education.com/worksheets http://pbskids.org/cyberchase/find- it/fractions/  The fraction think board
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	10. INTRODUCTION TO THIRDS AND FIFTHS.  Demonstrate a collection shared equally into 3 groups and a collection shared unequally, ask if all groups represent 1/3. Can they explain? Share collections of lollies/ cubes/ counters into 3 equal groups. Discuss thirds and the symbol. Record the results. Repeat for 1/5  Show the students an A4 paper divided unequally into 8, ask them if each part is 1/8. Give them an A4 piece of paper and ask them to demonstrate how it could be divide it into eighths. Explain  Write 1/8 and eighth on the parts.	Technical Vocabulary: eighths, represent,  Process: share, record notice, demonstrate, write	
D - Model and represent unit fraction, including ½, ¼, 1/3, 1/5 and their multiples to a complete whole.	Introduce unit fraction with definition. A unit fraction is fraction where the numerator is 1. Have the students hold up 1/5 fraction parts. How many do we need for 1 whole. Repeat for other fractions.  Introduce the Unifix fraction game- they roll a 1-10 die. Whatever numeral comes up becomes the unit fraction eg: 6, Then each unifix cube is 1/6. They explore how many 1/6 cubes they would need to make a whole. Give them a grid to record. What do you notice?  What would be your theory?  Can you prove it?  Unit fraction  How many multiples did you need?	Technical Vocabulary: unit fraction, multiple Complex sentence: I notice that	View video ABC Splash splash.abc.net.au  Read write and compare fractions.  REPLIENTS  ACADION  ACADIO

## Overview of language and examples used in the teaching, learning and assessing program

A summary of the language mostly pertaining to this substrand as used in the following teaching, learning and assessing program.

Oral Texts	Visual Texts and Symbols	Text Knowledge	Grammar Knowledge	Word Knowledge
Spoken Texts Participates in oral texts to explore understandings about our number system.  Verbal elements Pronounces unit fractions eg thirds, halves, quarters.  Speech functions Responds to statements /commands and asks questions when required. Describes fractions and learning using statements.  Social exchanges Collaborates with others  Explains strategies in small groups/whole class.  Reflects on strategies used.	Visuals in Multimodal texts  Symbolism Symbols to represent fractions eg ½,1/4,1/8, 1/5, 1/6, 1/3 <,>,=,≠  Semiotics Fraction wall Number line	Written texts: Label fractions.  Reference items It, they, this, these	Simple sentences This is a fraction.  Compound sentences There are x equal parts so each part is called a  Complex sentences I think this is a fifth because there are 5 equal parts.  Print Conventions setting out mathematically  Processes Action: divide, share, find, select, fold, share, mental: think, relational: equals, is, are Paired constructions with verb to be omitted. The larger the denominator (is), the smaller the fraction (is).  Multi word verb group One whole (circle, block, box of paperclips, basketball court) has been divided into equal parts  Simple present tense The basketball court has 3 equal parts.  Past tense for problematised stories I had 20 library books and gave each class  Nouns and Noun Groups classroom objects, shapes, collections  Comparative Language This part is smaller than	Technical Vocabulary whole, part fraction, collection, equal to, equivalent, numerator, denominator, vinculum, same as, theory, unit fraction, multiple, rule  relate, investigate, compare, record, order, justify, represent, test, label,  Ordinal numbers (regular and irregular) and fraction names (We say first instead of oneth, second instead of twoth.)

Appendix			